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# **fivenx Documentation**

***Release 2.2.1***

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**fgivenx** Functional Posterior Plotter

**Author** Will Handley

**Version** 2.2.1

**Homepage** <https://github.com/williamjameshandley/fgivenx>

**Documentation** <http://fgivenx.readthedocs.io/>





# CHAPTER 1

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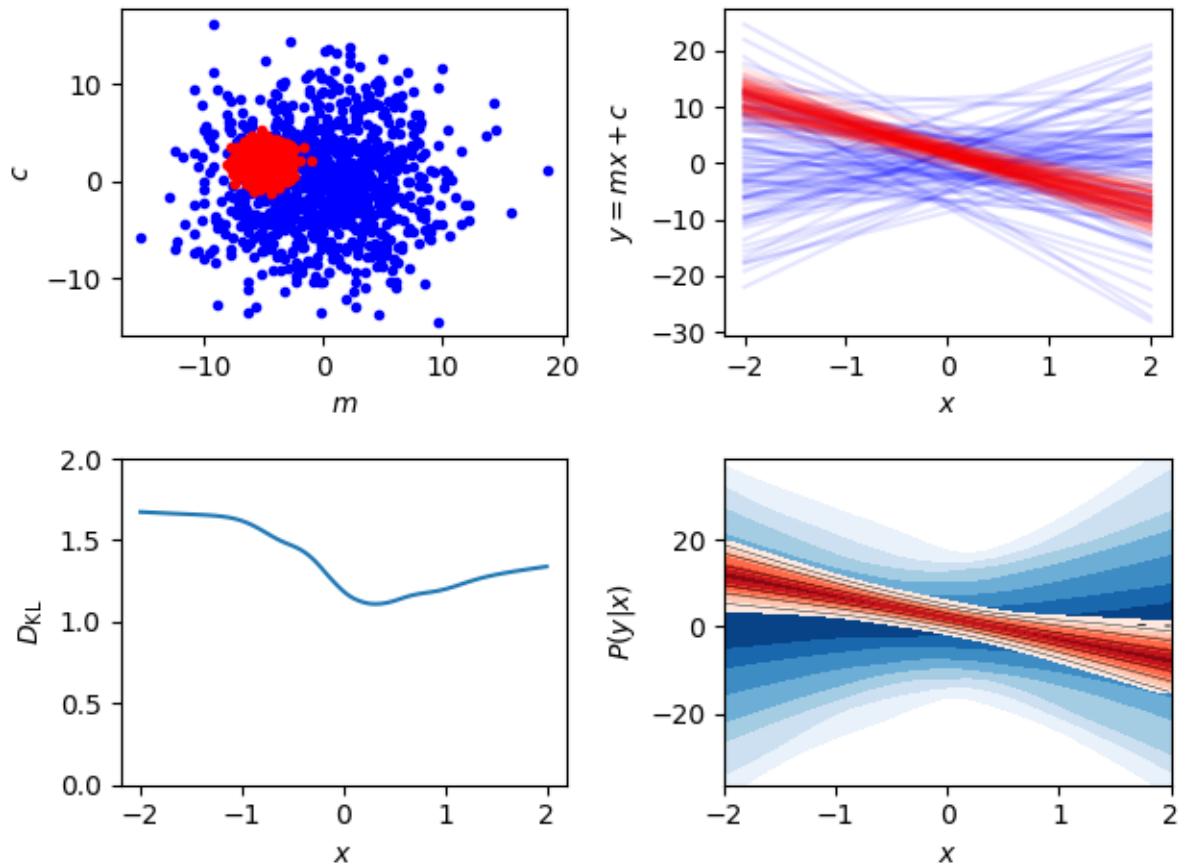
## Description

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`fgivenx` is a python package for plotting posteriors of functions. It is currently used in astronomy, but will be of use to any scientists performing Bayesian analyses which have predictive posteriors that are functions.

This package allows one to plot a predictive posterior of a function, dependent on sampled parameters. We assume one has a Bayesian posterior  $\text{Post}(\theta | D, M)$  described by a set of posterior samples  $\{\theta_i\} \sim \text{Post}$ . If there is a function parameterised by  $\theta$   $y = f(x; \theta)$ , then this script will produce a contour plot of the conditional posterior  $P(y | x, D, M)$  in the  $(x, y)$  plane.

The driving routines are `fgivenx.plot_contours`, `fgivenx.plot_lines` and `fgivenx.plot_dkl`. The code is compatible with `getdist`, and has a loading function provided by `fgivenx.samples_from_getdist_chains`.



# CHAPTER 2

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## Getting Started

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Users can install using pip:

```
pip install fgivenx
```

from source:

```
git clone https://github.com/williamjameshandley/fgivenx
cd fgivenx
python setup.py install --user
```

or for those on Arch linux it is available on the [AUR](#)

You can check that things are working by running the test suite (You may encounter warnings if the optional dependency `joblib` is not installed):

```
pip install pytest pytest-runner pytest-mpl
export MPLBACKEND=Agg
pytest <fgivenx-install-location>

# or, equivalently
git clone https://github.com/williamjameshandley/fgivenx
cd fgivenx
python setup.py test
```

Check the dependencies listed in the next section are installed. You can then use the `fgivenx` module from your scripts.

Some users of OSX or [Anaconda](#) may find `QueueManagerThread` errors if `Pillow` is not installed (run `pip install pillow`).

If you want to use parallelisation, have progress bars or `getdist` compatibility you should install the additional optional dependencies:

```
pip install joblib tqdm getdist
# or, equivalently
pip install -r requirements.txt
```

You may encounter warnings if you don't have the optional dependency `joblib` installed.

# CHAPTER 3

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## Dependencies

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Basic requirements:

- Python 2.7+ or 3.4+
- `matplotlib`
- `numpy`
- `scipy`

Documentation:

- `sphinx`
- `numpydoc`

Tests:

- `pytest`
- `pytest-mpl`

Optional extras:

- `joblib` (parallelisation) [+ `pillow` on some systems]
- `tqdm` (progress bars)
- `getdist` (reading of getdist compatible files)



# CHAPTER 4

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## Documentation

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Full Documentation is hosted at [ReadTheDocs](#). To build your own local copy of the documentation you'll need to install [sphinx](#). You can then run:

```
cd docs  
make html
```



# CHAPTER 5

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## Citation

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If you use `fgivenx` to generate plots for a publication, please cite as:

```
Handley, (2018). fgivenx: A Python package for functional posterior plotting . Journal of Open Source Software, 3(28), 849,  
https://doi.org/10.21105/joss.00849
```

or using the BibTeX:

```
@article{fgivenx,  
  doi = {10.21105/joss.00849},  
  url = {http://dx.doi.org/10.21105/joss.00849},  
  year = {2018},  
  month = {Aug},  
  publisher = {The Open Journal},  
  volume = {3},  
  number = {28},  
  author = {Will Handley},  
  title = {fgivenx: Functional Posterior Plotter},  
  journal = {The Journal of Open Source Software}  
}
```



# CHAPTER 6

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## Example Usage

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### 6.1 Plot user-generated samples

```
import numpy
import matplotlib.pyplot as plt
from fgivenx import plot_contours, plot_lines, plot_dkl

# Model definitions
# =====
# Define a simple straight line function, parameters theta=(m, c)
def f(x, theta):
    m, c = theta
    return m * x + c

numpy.random.seed(1)

# Posterior samples
nsamples = 1000
ms = numpy.random.normal(loc=-5, scale=1, size=nsamples)
cs = numpy.random.normal(loc=2, scale=1, size=nsamples)
samples = numpy.array([(m, c) for m, c in zip(ms, cs)]).copy()

# Prior samples
ms = numpy.random.normal(loc=0, scale=5, size=nsamples)
cs = numpy.random.normal(loc=0, scale=5, size=nsamples)
prior_samples = numpy.array([(m, c) for m, c in zip(ms, cs)]).copy()

# Set the x range to plot on
xmin, xmax = -2, 2
nx = 100
x = numpy.linspace(xmin, xmax, nx)
```

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```

# Set the cache
cache = 'cache/test'
prior_cache = cache + '_prior'

# Plotting
# -----
fig, axes = plt.subplots(2, 2)

# Sample plot
# -----
ax_samples = axes[0, 0]
ax_samples.set_ylabel(r'$c$')
ax_samples.set_xlabel(r'$m$')
ax_samples.plot(prior_samples.T[0], prior_samples.T[1], 'b.')
ax_samples.plot(samples.T[0], samples.T[1], 'r.')

# Line plot
# -----
ax_lines = axes[0, 1]
ax_lines.set_ylabel(r'$y = m x + c$')
ax_lines.set_xlabel(r'$x$')
plot_lines(f, x, prior_samples, ax_lines, color='b', cache=prior_cache)
plot_lines(f, x, samples, ax_lines, color='r', cache=cache)

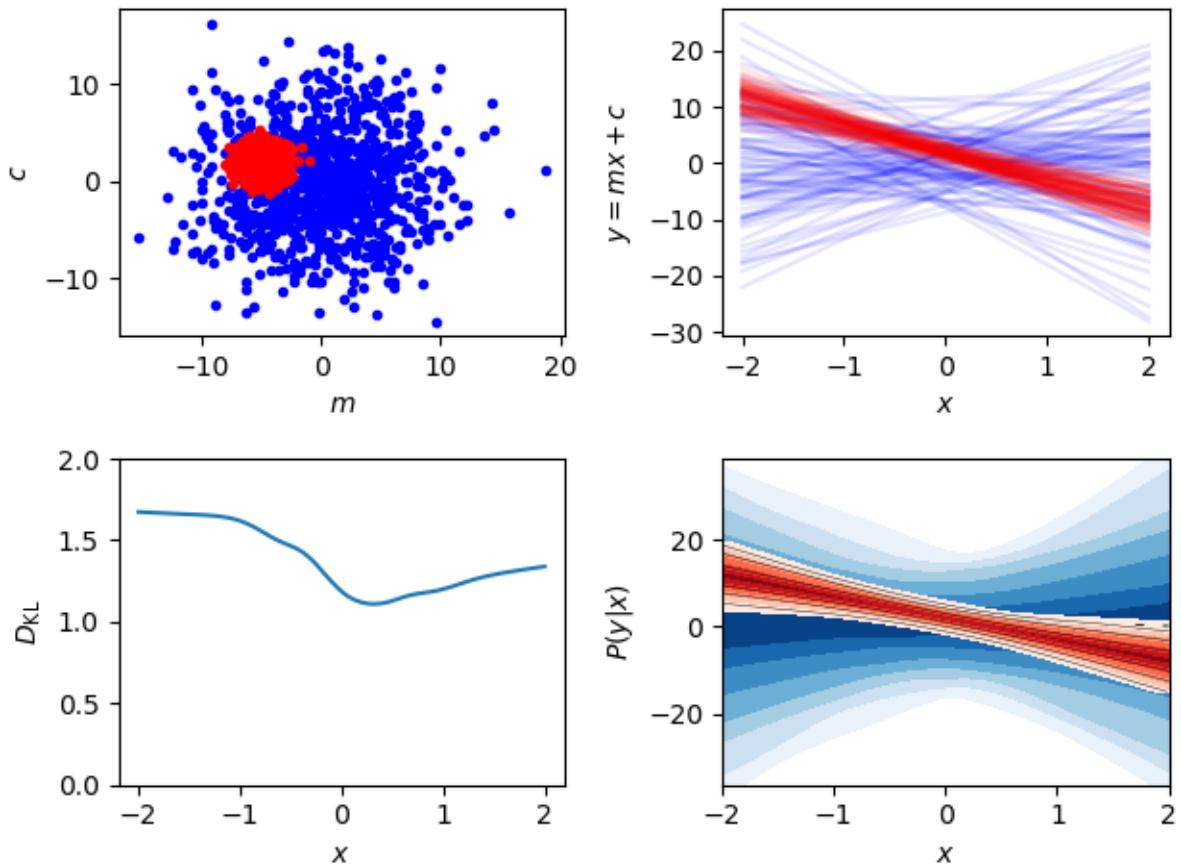
# Predictive posterior plot
# -----
ax_fgivenx = axes[1, 1]
ax_fgivenx.set_ylabel(r'$P(y|x)$')
ax_fgivenx.set_xlabel(r'$x$')
cbar = plot_contours(f, x, prior_samples, ax_fgivenx,
                     colors=plt.cm.Blues_r, lines=False,
                     cache=prior_cache)
cbar = plot_contours(f, x, samples, ax_fgivenx, cache=cache)

# DKL plot
# -----
ax_dkl = axes[1, 0]
ax_dkl.set_ylabel(r'$D_{\text{KL}}(\mathcal{P}||\mathcal{Q})$')
ax_dkl.set_xlabel(r'$x$')
ax_dkl.set_ylim(bottom=0, top=2.0)
plot_dkl(f, x, samples, prior_samples, ax_dkl,
         cache=cache, prior_cache=prior_cache)

ax_lines.get_shared_x_axes().join(ax_lines, ax_fgivenx, ax_dkl)

fig.tight_layout()
fig.savefig('plot.png')

```



## 6.2 Plot GetDist chains

```

import numpy
import matplotlib.pyplot as plt
from fgivenx import plot_contours, samples_from_getdist_chains

file_root = './plik_HM_TT_lowl/base_plikHM_TT_lowl'
samples, weights = samples_from_getdist_chains(['logA', 'ns'], file_root)

def PPS(k, theta):
    logA, ns = theta
    return logA + (ns - 1) * numpy.log(k)

k = numpy.logspace(-4, 1, 100)
cbar = plot_contours(PPS, k, samples, weights=weights)
cbar = plt.colorbar(cbar, ticks=[0, 1, 2, 3])
cbar.set_ticklabels(['', r'$1\sigma$', r'$2\sigma$', r'$3\sigma$'])

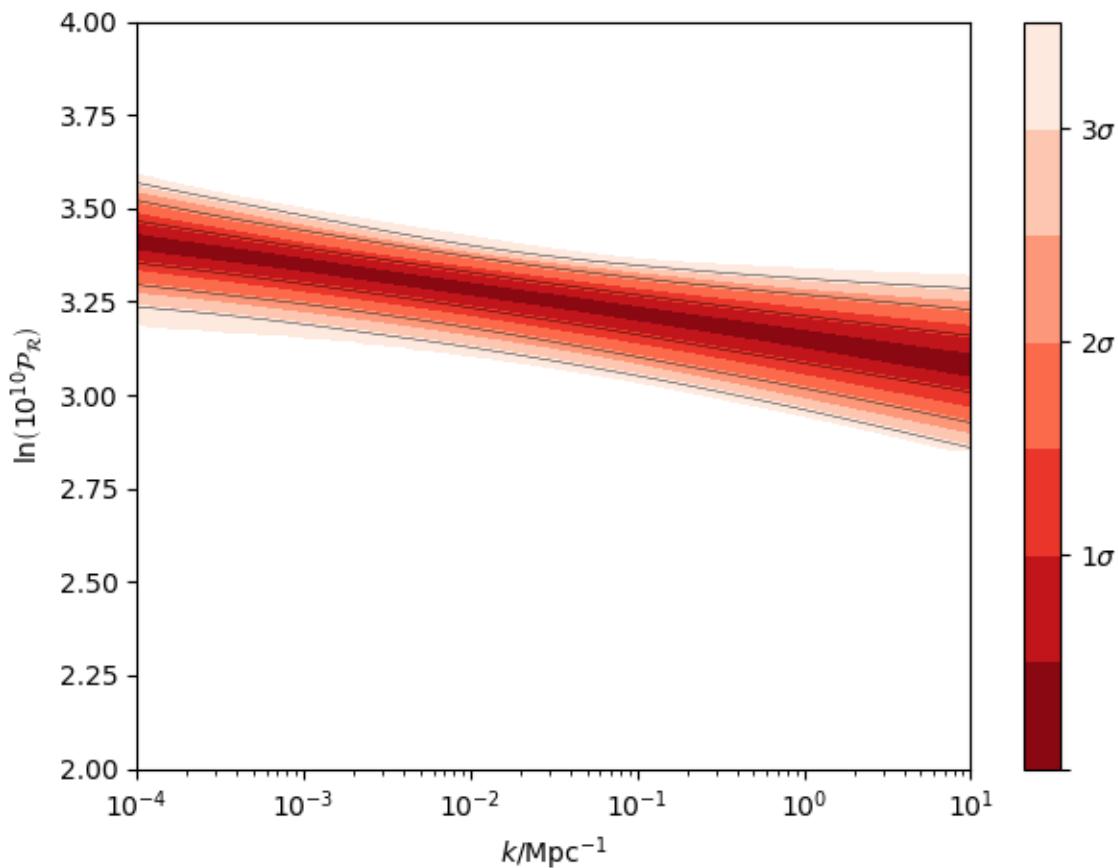
plt.xscale('log')
plt.ylim(2, 4)
plt.ylabel(r'$\ln\left(10^{10}\mathcal{P}_R\right)$')
plt.xlabel(r'$k / \mathrm{Mpc}^{-1}$')
plt.tight_layout()

```

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```
plt.savefig('planck.png')
```



# CHAPTER 7

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## Contributing

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Want to contribute to `fivenx`? Awesome! There are many ways you can contribute via the [GitHub repository](<https://github.com/williamjameshandley/fivenx>), see below.

### 7.1 Opening issues

Open an issue to report bugs or to propose new features.

### 7.2 Proposing pull requests

Pull requests are very welcome. Note that if you are going to propose drastic changes, be sure to open an issue for discussion first, to make sure that your PR will be accepted before you spend effort coding it.



# CHAPTER 8

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## Changelog

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- v2.2.0** Paper accepted
- v2.1.17** 100% coverage
- v2.1.16** Tests fixes
- v2.1.15** Additional plot tests
- v2.1.13** Further bug fix in test suite for image comparison
- v2.1.12** Bug fix in test suite for image comparison
- v2.1.11** Documentation upgrades
- v2.1.10** Added changelog



# CHAPTER 9

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## fgivenx package

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### 9.1 Module contents

The main driving routines for this package are:

- *plot\_contours*
- *plot\_lines*
- *plot\_dkl*
- *samples\_from\_getdist\_chains*

Example import and usage:

```
>>> import numpy
>>> from fgivenx import plot_contours, plot_lines, ...
   <samples_from_getdist_chains
>>>
>>> file_root = '/my/getdist/file/root'
>>> params = ['m', 'c']
>>> samples = samples_from_getdist_chains(params, file_root)
>>> x = numpy.linspace(-1, 1, 100)
>>>
>>> def f(x, theta):
   >>>     m, c = params
   >>>     y = m * x + c
   >>>     return y
>>>
>>> plot_contours(f, x, samples)
```

## 9.2 Submodules

### 9.3 fgivenx.drivers module

This module provides utilities for computing the grid for contours of a function reconstruction plot.

#### Required ingredients:

- sampled posterior probability distribution  $P(\theta)$
- independent variable  $x$
- dependent variable  $y$
- functional form  $y = f(x; \theta)$  parameterised by  $\theta$

Assuming that you have obtained samples of  $\theta$  from an MCMC process, we aim to compute the density:

$$\begin{aligned} P(y|x) &= \int P(y = f(x; \theta)|x, \theta)P(\theta)d\theta \\ &= \int \delta(y - f(x; \theta))P(\theta)d\theta \end{aligned}$$

which gives our degree of knowledge for each  $y = f(x; \theta)$  value given an  $x$  value.

In fact, for a more representative plot, we are not actually interested in the value of the probability density above, but in fact require the “iso-probability posterior mass”

$$\text{pmf}(y|x) = \int_{P(y'|x) < P(y|x)} P(y'|x)dy'$$

We thus need to compute this function on a rectangular grid of  $x$  and  $y$ .

`fgivenx.drivers.compute_dkl(f, x, samples, prior_samples, **kwargs)`

Compute the Kullback-Leibler divergence at each value of  $x$  for the prior and posterior defined by `prior_samples` and `samples`.

#### Parameters

**f: function** function  $f(x; \theta)$  (or list of functions for each model) with dependent variable  $x$ , parameterised by  $\theta$ .

**x: 1D array-like**  $x$  values to evaluate  $f(x; \theta)$  at.

**samples, prior\_samples: 2D array-like**  $\theta$  samples (or list of  $\theta$  samples) from posterior and prior to evaluate  $f(x; \theta)$  at. `shape = (nsamples, npars)`

**logZ: 1D array-like, optional** log-evidences of each model if multiple models are passed. Should be same length as the list `f`, and need not be normalised. Default: `numpy.ones_like(f)`

**weights, prior\_weights: 1D array-like, optional** sample weights (or list of weights), if desired. Should have length same as `samples.shape[0]`. Default: `numpy.ones_like(samples)`

**ntrim: int, optional** Approximate number of samples to trim down to, if desired. Useful if the posterior is dramatically oversampled. Default: None

**cache, prior\_cache: str, optional** File roots for saving previous calculations for re-use

**parallel, tqdm\_args:** see docstring for `fgivenx.parallel.parallel_apply()`

**kwargs: further keyword arguments** Any further keyword arguments are plotting keywords that are passed to `fgivenx.plot.plot()`.

**Returns**

**1D numpy array:** dkl values at each value of  $x$ .

```
fgivenx.drivers.compute_pmf(f, x, samples, **kwargs)
```

Compute the probability mass function given  $x$  at a range of  $x$  values for  $y = f(x|\theta)$

$$P(y|x) = \int P(y = f(x; \theta)|x, \theta)P(\theta)d\theta$$

$$\text{pmf}(y|x) = \int_{P(y'|x) < P(y|x)} P(y'|x)dy'$$

Additionally, if a list of log-evidences are passed, along with list of functions, samples and optional weights it marginalises over the models according to the evidences.

**Parameters**

**f: function** function  $f(x; \theta)$  (or list of functions for each model) with dependent variable  $x$ ,

parameterised by  $\theta$ .

**x: 1D array-like**  $x$  values to evaluate  $f(x; \theta)$  at.

**samples: 2D array-like**  $\theta$  samples (or list of  $\theta$  samples) to evaluate  $f(x; \theta)$  at.  $\text{shape} = (nsamples, npars)$

**logZ: 1D array-like, optional** log-evidences of each model if multiple models are passed.  
Should be same length as the list  $f$ , and need not be normalised. Default: `numpy.ones_like(f)`

**weights: 1D array-like, optional** sample weights (or list of weights), if desired. Should have length same as  $\text{samples.shape[0]}$ . Default: `numpy.ones_like(samples)`

**ny: int, optional** Resolution of  $y$  axis. Default: 100

**y: array-like, optional** Explicit descriptor of  $y$  values to evaluate. Default:  
`numpy.linspace(min(f), max(f), ny)`

**ntrim: int, optional** Approximate number of samples to trim down to, if desired. Useful if the posterior is dramatically oversampled. Default: None

**cache: str, optional** File root for saving previous calculations for re-use

**parallel, tqdm\_args:** see docstring for `fgivenx.parallel.parallel_apply()`

**Returns**

**1D numpy.array:**  $y$  values pmf is computed at  $\text{shape}=(\text{len}(y))$  or  $ny$

**2D numpy.array:** pmf values at each  $x$  and  $y$   $\text{shape}=(\text{len}(x), \text{len}(y))$

```
fgivenx.drivers.compute_samples(f, x, samples, **kwargs)
```

Apply the function(s)  $f(x; \theta)$  to the arrays defined in  $x$  and  $\text{samples}$ . Has options for weighting, trimming, cacheing & parallelising.

Additionally, if a list of log-evidences are passed, along with list of functions, samples and optional weights it marginalises over the models according to the evidences.

**Parameters**

**f: function** function  $f(x; \theta)$  (or list of functions for each model) with dependent variable  $x$ , parameterised by  $\theta$ .

**x: 1D array-like**  $x$  values to evaluate  $f(x; \theta)$  at.

**samples: 2D array-like**  $\theta$  samples (or list of  $\theta$  samples) to evaluate  $f(x; \theta)$  at.  $\text{shape} = (nsamples, npars)$

**logZ: 1D array-like, optional** log-evidences of each model if multiple models are passed.  
Should be same length as the list  $f$ , and need not be normalised. Default: `numpy.ones_like(f)`

**weights: 1D array-like, optional** sample weights (or list of weights), if desired. Should have length same as `samples.shape[0]`. Default: `numpy.ones_like(samples)`

**ntrim: int, optional** Approximate number of samples to trim down to, if desired. Useful if the posterior is dramatically oversampled. Default: None

**cache: str, optional** File root for saving previous calculations for re-use. Default: None

**parallel, tqdm\_args:** see docstring for `fgivenx.parallel.parallel_apply()`

### Returns

**2D numpy.array** Evaluate the function  $f$  at each  $x$  value and each theta. Equivalent to  $\{f(x_i, \theta) \text{ for } \theta \text{ in samples}\} \text{ for } x_i \text{ in } x\}$

`fgivenx.drivers.plot_contours(f, x, samples, ax=None, **kwargs)`

Plot the probability mass function given  $x$  at a range of  $y$  values for  $y = f(x|\theta)$

$$P(y|x) = \int P(y = f(x; \theta)|x, \theta)P(\theta)d\theta$$

$$\text{pmf}(y|x) = \int_{P(y'|x) < P(y|x)} P(y'|x)dy'$$

Additionally, if a list of log-evidences are passed, along with list of functions, and list of samples, this function plots the probability mass function for all models marginalised according to the evidences.

### Parameters

**f: function** function  $f(x; \theta)$  (or list of functions for each model) with dependent variable  $x$ , parameterised by  $\theta$ .

**x: 1D array-like**  $x$  values to evaluate  $f(x; \theta)$  at.

**samples: 2D array-like**  $\theta$  samples (or list of  $\theta$  samples) to evaluate  $f(x; \theta)$  at. `shape = (nsamples, npars)`

**ax: axes object, optional** `matplotlib.axes._subplots.AxesSubplot` to plot the contours onto. If unsupplied, then `matplotlib.pyplot.gca()` is used to get the last axis used, or create a new one.

**logZ: 1D array-like, optional** log-evidences of each model if multiple models are passed. Should be same length as the list  $f$ , and need not be normalised. Default: `numpy.ones_like(f)`

**weights: 1D array-like, optional** sample weights (or list of weights), if desired. Should have length same as `samples.shape[0]`. Default: `numpy.ones_like(samples)`

**ny: int, optional** Resolution of y axis. Default: 100

**y: array-like, optional** Explicit descriptor of  $y$  values to evaluate. Default: `numpy.linspace(min(f), max(f), ny)`

**ntrim: int, optional** Approximate number of samples to trim down to, if desired. Useful if the posterior is dramatically oversampled. Default: None

**cache: str, optional** File root for saving previous calculations for re-use

**parallel, tqdm\_args:** see docstring for `fgivenx.parallel.parallel_apply()`

**kwargs: further keyword arguments** Any further keyword arguments are plotting keywords that are passed to `fgivenx.plot.plot()`.

### Returns

**cbar: color bar** `matplotlib.contour.QuadContourSet` Colors to create a global colour bar

---

`fgivenx.drivers.plot_dkl(f, x, samples, prior_samples, ax=None, **kwargs)`

Plot the Kullback-Leibler divergence at each value of  $x$  for the prior and posterior defined by `prior_samples` and `samples`.

Let the posterior be:

$$P(y|x) = \int P(y = f(x; \theta)|x, \theta)P(\theta)d\theta$$

and the prior be:

$$Q(y|x) = \int P(y = f(x; \theta)|x, \theta)Q(\theta)d\theta$$

then the Kullback-Leibler divergence at each  $x$  is defined by

$$D_{KL}(x) = \int P(y|x) \ln \left[ \frac{Q(y|x)}{P(y|x)} \right] dy$$

Additionally, if a list of log-evidences are passed, along with list of functions, and list of samples, this function plots the Kullback-Leibler divergence for all models marginalised according to the evidences.

#### Parameters

**f: function** function  $f(x; \theta)$  (or list of functions for each model) with dependent variable  $x$ , parameterised by  $\theta$ .

**x: 1D array-like**  $x$  values to evaluate  $f(x; \theta)$  at.

**samples, prior\_samples: 2D array-like**  $\theta$  samples (or list of  $\theta$  samples) from posterior and prior to evaluate  $f(x; \theta)$  at. `shape = (nsamples, npars)`

**ax: axes object, optional** `matplotlib.axes._subplots.AxesSubplot` to plot the contours onto. If unsupplied, then `matplotlib.pyplot.gca()` is used to get the last axis used, or create a new one.

**logZ: 1D array-like, optional** log-evidences of each model if multiple models are passed. Should be same length as the list `f`, and need not be normalised. Default: `numpy.ones_like(f)`

**weights, prior\_weights: 1D array-like, optional** sample weights (or list of weights), if desired. Should have length same as `samples.shape[0]`. Default: `numpy.ones_like(samples)`

**ntrim: int, optional** Approximate number of samples to trim down to, if desired. Useful if the posterior is dramatically oversampled. Default: None

**cache, prior\_cache: str, optional** File roots for saving previous calculations for re-use

**parallel, tqdm\_args:** see docstring for `fgivenx.parallel.parallel_apply()`

**kwargs: further keyword arguments** Any further keyword arguments are plotting keywords that are passed to `fgivenx.plot.plot()`.

`fgivenx.drivers.plot_lines(f, x, samples, ax=None, **kwargs)`

Plot a representative set of functions to sample

Additionally, if a list of log-evidences are passed, along with list of functions, and list of samples, this function plots the probability mass function for all models marginalised according to the evidences.

#### Parameters

**f: function** function  $f(x; \theta)$  (or list of functions for each model) with dependent variable  $x$ , parameterised by  $\theta$ .

**x: 1D array-like**  $x$  values to evaluate  $f(x; \theta)$  at.

**samples: 2D array-like**  $\theta$  samples (or list of  $\theta$  samples) to evaluate  $f(x; \theta)$  at. `shape = (nsamples, npars)`

**ax: axes object, optional** `matplotlib.axes._subplots.AxesSubplot` to plot the contours onto. If unsupplied, then `matplotlib.pyplot.gca()` is used to get the last axis used, or create a new one.

**logZ: 1D array-like, optional** log-evidences of each model if multiple models are passed. Should be same length as the list `f`, and need not be normalised. Default: `numpy.ones_like(f)`

**weights: 1D array-like, optional** sample weights (or list of weights), if desired. Should have length same as `samples.shape[0]`. Default: `numpy.ones_like(samples)`

**ntrim: int, optional** Approximate number of samples to trim down to, if desired. Useful if the posterior is dramatically oversampled. Default: None

**cache: str, optional** File root for saving previous calculations for re-use

**parallel, tqdm\_args:** see docstring for `fgivenx.parallel.parallel_apply()`

**kwargs: further keyword arguments** Any further keyword arguments are plotting keywords that are passed to `fgivenx.plot.plot_lines()`.

## 9.4 fgivenx.dkl module

`fgivenx.dkl.DKL(arrays)`

Compute the Kullback-Leibler divergence from one distribution Q to another P, where Q and P are represented by a set of samples.

### Parameters

**arrays: tuple(1D numpy.array, 1D numpy.array)** samples defining distributions P & Q respectively

### Returns

**float:** Kullback Leibler divergence.

`fgivenx.dkl.compute_dkl(fsamps, prior_fsamps, **kwargs)`

Compute the Kullback Leibler divergence for function samples for posterior and prior pre-calculated at a range of x values.

### Parameters

**fsamps: 2D numpy.array** Posterior function samples, as computed by `fgivenx.compute_samples()`

**prior\_fsamps: 2D numpy.array** Prior function samples, as computed by `fgivenx.compute_samples()`

**parallel, tqdm\_kwargs: optional** see docstring for `fgivenx.parallel.parallel_apply()`.

**cache: str, optional** File root for saving previous calculations for re-use.

### Returns

**1D numpy.array:** Kullback-Leibler divergences at each value of x. `shape=(len(fsamps))`

## 9.5 fgivenx.io module

**class** `fgivenx.io.Cache(file_root)`  
Bases: `object`

Caching tool for saving recomputation.

### Parameters

**file\_root:** str cached values are saved in file\_root.pkl

### Methods

<code>check(self, \*args)</code>	Check that the arguments haven't changed since the last call.
<code>load(self)</code>	Load cache from file using pickle.
<code>save(self, \*args)</code>	Save cache to file using pickle.

**check (self, \*args)**

Check that the arguments haven't changed since the last call.

### Parameters

**\*args:** All but the last argument are inputs to the cached function. The last is the actual value of the function.

### Returns

**If arguments unchanged:** return the cached answer

**else:** indicate recomputation required by throwing a `CacheException`.

**load (self)**

Load cache from file using pickle.

**save (self, \*args)**

Save cache to file using pickle.

### Parameters

**\*args:** All but the last argument are inputs to the cached function. The last is the actual value of the function.

**exception fgivenx.io.CacheChanged (file\_root)**

Bases: `fgivenx.io.CacheException`

Exception to indicate the cache has changed.

**exception fgivenx.io.CacheException**

Bases: `exceptions.Exception`

Base exception to indicate cache errors

**calling\_function (self)**

Get the name of the function calling this cache.

**exception fgivenx.io.CacheMissing (file\_root)**

Bases: `fgivenx.io.CacheException`

Exception to indicate the cache does not exist.

**exception fgivenx.io.CacheOK (file\_root)**

Bases: `fgivenx.io.CacheException`

Exception to indicate the cache can be used.

## 9.6 fgivenx.mass module

Utilities for computing the probability mass function.

`fgivenx.mass.PMF(samples, y)`

Compute the probability mass function.

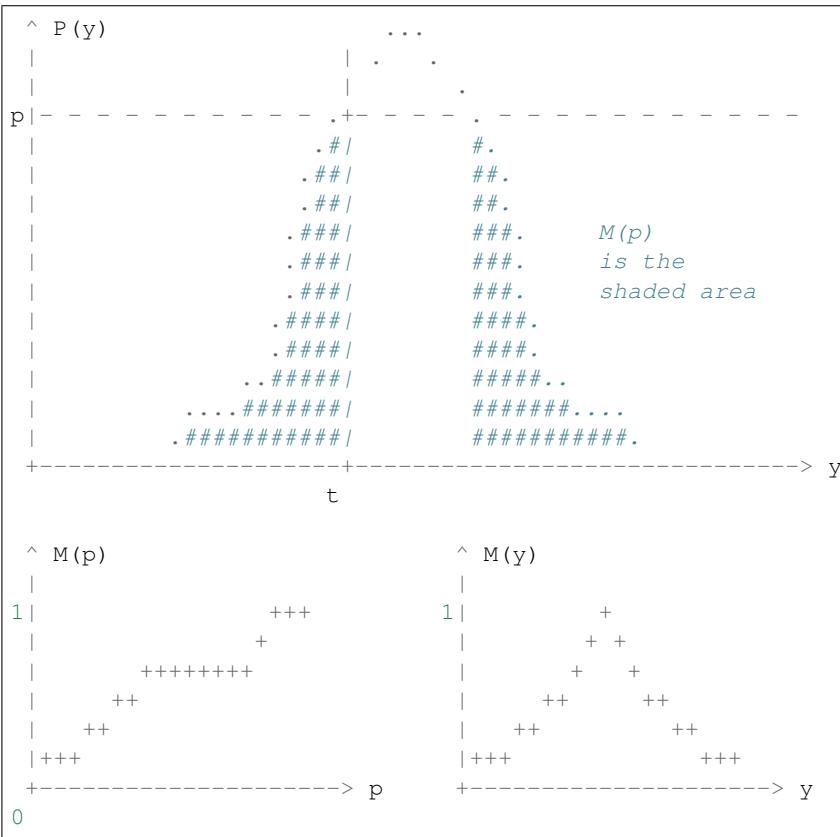
The set of samples defines a probability density  $P(y)$ , which is computed using a kernel density estimator.

From  $P(y)$  we define:

$$\text{pmf}(p) = \int_{P(y) < p} P(y) dy$$

This is the cumulative distribution function expressed as a function of the probability

We aim to compute  $M(y)$ , which indicates the amount of probability contained outside the iso-probability contour passing through  $y$ :



### Parameters

**samples: array-like** Array of samples from a probability density  $P(y)$ .

**y: array-like (optional)** Array to evaluate the PDF at

### Returns

**1D numpy.array:** PMF evaluated at each y value

`fgivenx.mass.compute_pmf(fsamps, y, **kwargs)`

Compute the pmf defined by fsamps at each x for each y.

### Parameters

---

**fsamps:** **2D array-like** array of function samples, as returned by `fgivenx.compute_samples()`

**y:** **1D array-like** y values to evaluate the PMF at

**parallel, tqdm\_kwarg:** **optional** see docstring for `fgivenx.parallel.parallel_apply()`.

**Returns**

**2D numpy.array** probability mass function at each x for each y `shape=(len(fsamps), len(y))`

## 9.7 fgivenx.parallel module

`fgivenx.parallel.parallel_apply(f, array, **kwargs)`

Apply a function to an array with openmp parallelisation.

Equivalent to `[f(x) for x in array]`, but parallelised if required.

**Parameters**

**f:** **function** Univariate function to apply to each element of array

**array:** **array-like** Array to apply f to

**parallel:** **int or bool, optional** int > 0: number of processes to parallelise over

int < 0 or bool=True: use OMP\_NUM\_THREADS to choose parallelisation

bool=False or int=0: do not parallelise

**tqdm\_kwarg:** **dict, optional** additional kwargs for tqdm progress bars.

**precurry:** **tuple, optional** immutable arguments to pass to f before x, i.e. `[f(precurry,x) for x in array]`

**postcurry:** **tuple, optional** immutable arguments to pass to f after x i.e. `[f(x,postcurry) for x in array]`

**Returns**

**list:** `[f(precurry,x,postcurry) for x in array]` parallelised according to parallel

## 9.8 fgivenx.plot module

`fgivenx.plot.plot(x, y, z, ax=None, **kwargs)`

Plot iso-probability mass function, converted to sigmas.

**Parameters**

**x, y, z** [numpy arrays] Same as arguments to `matplotlib.pyplot.contour()`

**ax:** **axes object, optional** `matplotlib.axes._subplots.AxesSubplot` to plot the contours onto. If unsupplied, then `matplotlib.pyplot.gca()` is used to get the last axis used, or create a new one.

**colors:** **color scheme, optional** `matplotlib.colors.LinearSegmentedColormap` Color scheme to plot with. Recommend plotting in reverse (Default: `matplotlib.pyplot.cm.Reds_r`)

**smooth:** **float, optional** Percentage by which to smooth the contours. (Default: no smoothing)

**contour\_line\_levels: List[float], optional** Contour lines to be plotted. (Default: [1,2])  
**linewidths: float, optional** Thickness of contour lines. (Default: 0.3)  
**contour\_color\_levels: List[float], optional** Contour color levels. (Default: `numpy.arange(0, contour_line_levels[-1] + 1, fineness)`)  
**fineness: float, optional** Spacing of contour color levels. (Default: 0.1)  
**lines: bool, optional** (Default: True)  
**rasterize\_contours: bool, optional** Rasterize the contours while keeping the lines, text etc in vector format. Useful for reducing file size bloat and making printing easier when you have dense contours. (Default: False)

#### Returns

**cbar: color bar** `matplotlib.contour.QuadContourSet` Colors to create a global colour bar

`fgivenx.plot.plot_lines(x, fsamps, ax=None, downsample=100, **kwargs)`  
Plot function samples as a set of line plots.

#### Parameters

**x: 1D array-like** x values to plot  
**fsamps: 2D array-like** set of functions to plot at each x. As returned by `fgivenx.compute_samples()`  
**ax: axes object** `matplotlib.pyplot.ax` to plot on.  
**downsample: int, optional** Reduce the number of samples to a viewable quantity. (Default 100)  
**any other keywords are passed to :meth:`matplotlib.pyplot.ax.plot`**

## 9.9 fgivenx.samples module

`fgivenx.samples.compute_samples(f, x, samples, **kwargs)`  
Apply  $f(x, \theta)$  to x array and theta in samples.

#### Parameters

**f: function** list of functions  $f(x; \theta)$  with dependent variable  $x$ , parameterised by  $\theta$ .  
**x: 1D array-like** x values to evaluate  $f(x; \theta)$  at.  
**samples: 2D array-like** list of theta samples to evaluate  $f(x; \theta)$  at. `shape = (nfunc, nsamples, npars)`  
**parallel, tqdm\_kwargs: optional** see docstring for `fgivenx.parallel.parallel_apply()`  
**cache: str, optional** File root for saving previous calculations for re-use default None

#### Returns

**2D numpy.array:** samples at each x. `shape=(len(x), len(samples),)`

`fgivenx.samples.samples_from_getdist_chains(params, file_root, latex=False, **kwargs)`  
Extract samples and weights from getdist chains.

#### Parameters

**params: list(str)** Names of parameters to be supplied to second argument of f(x|theta).

**file\_root: str, optional** Root name for getdist chains files. This variable automatically defines:  
- chains\_file = file\_root.txt - paramnames\_file = file\_root.paramnames but can be overridden by chains\_file or paramnames\_file.

**latex: bool, optional** Also return an array of latex strings for those paramnames.

Any additional keyword arguments are forwarded onto getdist, e.g.

```
samples_from_getdist_chains(params, file_root, settings={'ignore_rows':0.5})
```

#### Returns

**samples: numpy.array** 2D Array of samples. *shape=(len(samples), len(params))*

**weights: numpy.array** Array of weights. *shape = (len(params),)*

**latex: list(str), optional** list of latex strings for each parameter (if latex is provided as an argument)



# CHAPTER 10

---

## fgivenx: Functional Posterior Plotter

---

**fgivenx** Functional Posterior Plotter

**Author** Will Handley

**Version** 2.2.1

**Homepage** <https://github.com/williamjameshandley/fgivenx>

**Documentation** <http://fgivenx.readthedocs.io/>

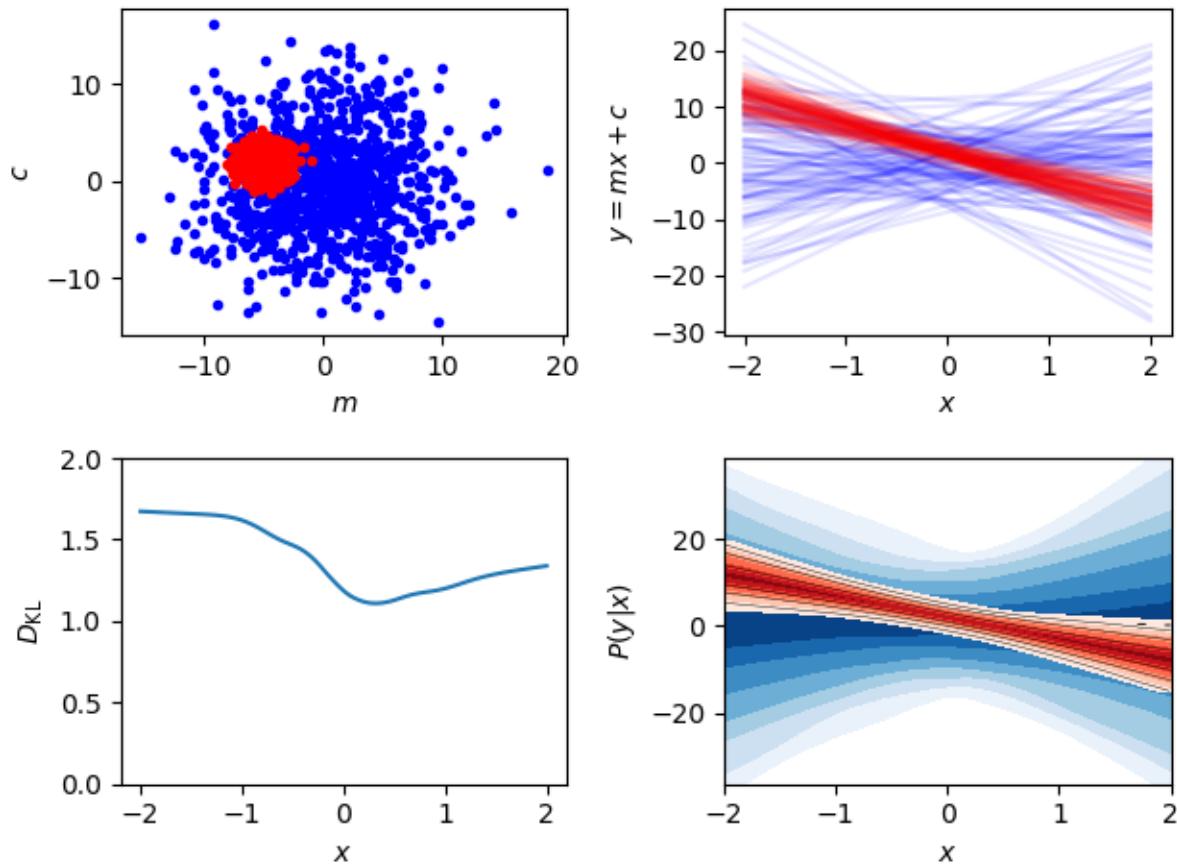


### 10.1 Description

`fgivenx` is a python package for plotting posteriors of functions. It is currently used in astronomy, but will be of use to any scientists performing Bayesian analyses which have predictive posteriors that are functions.

This package allows one to plot a predictive posterior of a function, dependent on sampled parameters. We assume one has a Bayesian posterior  $\text{Post}(\theta | D, M)$  described by a set of posterior samples  $\{\theta_i\} \sim \text{Post}$ . If there is a function parameterised by  $\theta$   $y = f(x; \theta)$ , then this script will produce a contour plot of the conditional posterior  $P(y | x, D, M)$  in the  $(x, y)$  plane.

The driving routines are `fgivenx.plot_contours`, `fgivenx.plot_lines` and `fgivenx.plot_dkl`. The code is compatible with `getdist`, and has a loading function provided by `fgivenx.samples_from_getdist_chains`.



## 10.2 Getting Started

Users can install using pip:

```
pip install fgivenx
```

from source:

```
git clone https://github.com/williamjameshandley/fgivenx
cd fgivenx
python setup.py install --user
```

or for those on [Arch linux](#) it is available on the [AUR](#)

You can check that things are working by running the test suite (You may encounter warnings if the optional dependency `joblib` is not installed):

```
pip install pytest pytest-runner pytest-mpl
export MPLBACKEND=Agg
pytest <fgivenx-install-location>
```

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```
# or, equivalently
git clone https://github.com/williamjameshandley/fgivenx
cd fgivenx
python setup.py test
```

Check the dependencies listed in the next section are installed. You can then use the `fgivenx` module from your scripts.

Some users of OSX or Anaconda may find `QueueManagerThread` errors if `Pillow` is not installed (run `pip install pillow`).

If you want to use parallelisation, have progress bars or `getdist` compatibility you should install the additional optional dependencies:

```
pip install joblib tqdm getdist
# or, equivalently
pip install -r requirements.txt
```

You may encounter warnings if you don't have the optional dependency `joblib` installed.

## 10.3 Dependencies

Basic requirements:

- Python 2.7+ or 3.4+
- `matplotlib`
- `numpy`
- `scipy`

Documentation:

- `sphinx`
- `numpydoc`

Tests:

- `pytest`
- `pytest-mpl`

Optional extras:

- `joblib` (parallelisation) [+ `pillow` on some systems]
- `tqdm` (progress bars)
- `getdist` (reading of `getdist` compatible files)

## 10.4 Documentation

Full Documentation is hosted at [ReadTheDocs](#). To build your own local copy of the documentation you'll need to install `sphinx`. You can then run:

```
cd docs  
make html
```

## 10.5 Citation

If you use `fgivenx` to generate plots for a publication, please cite as:

```
Handley, (2018). fgivenx: A Python package for functional posterior plotting . Journal of Open Source Software, 3(28), 849,  
https://doi.org/10.21105/joss.00849
```

or using the BibTeX:

```
@article{fgivenx,  
    doi = {10.21105/joss.00849},  
    url = {http://dx.doi.org/10.21105/joss.00849},  
    year = {2018},  
    month = {Aug},  
    publisher = {The Open Journal},  
    volume = {3},  
    number = {28},  
    author = {Will Handley},  
    title = {fgivenx: Functional Posterior Plotter},  
    journal = {The Journal of Open Source Software}  
}
```

## 10.6 Example Usage

### 10.6.1 Plot user-generated samples

```
import numpy  
import matplotlib.pyplot as plt  
from fgivenx import plot_contours, plot_lines, plot_dkl  
  
# Model definitions  
# ======  
# Define a simple straight line function, parameters theta=(m, c)  
def f(x, theta):  
    m, c = theta  
    return m * x + c  
  
numpy.random.seed(1)  
  
# Posterior samples  
nsamples = 1000  
ms = numpy.random.normal(loc=-5, scale=1, size=nsamples)  
cs = numpy.random.normal(loc=2, scale=1, size=nsamples)  
samples = numpy.array([(m, c) for m, c in zip(ms, cs)]).copy()
```

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```

# Prior samples
ms = numpy.random.normal(loc=0, scale=5, size=nsamples)
cs = numpy.random.normal(loc=0, scale=5, size=nsamples)
prior_samples = numpy.array([(m, c) for m, c in zip(ms, cs)]).copy()

# Set the x range to plot on
xmin, xmax = -2, 2
nx = 100
x = numpy.linspace(xmin, xmax, nx)

# Set the cache
cache = 'cache/test'
prior_cache = cache + '_prior'

# Plotting
# -----
fig, axes = plt.subplots(2, 2)

# Sample plot
# -----
ax_samples = axes[0, 0]
ax_samples.set_ylabel(r'$c$')
ax_samples.set_xlabel(r'$m$')
ax_samples.plot(prior_samples.T[0], prior_samples.T[1], 'b.')
ax_samples.plot(samples.T[0], samples.T[1], 'r.')

# Line plot
# -----
ax_lines = axes[0, 1]
ax_lines.set_ylabel(r'$y = m x + c$')
ax_lines.set_xlabel(r'$x$')
plot_lines(f, x, prior_samples, ax_lines, color='b', cache=prior_cache)
plot_lines(f, x, samples, ax_lines, color='r', cache=cache)

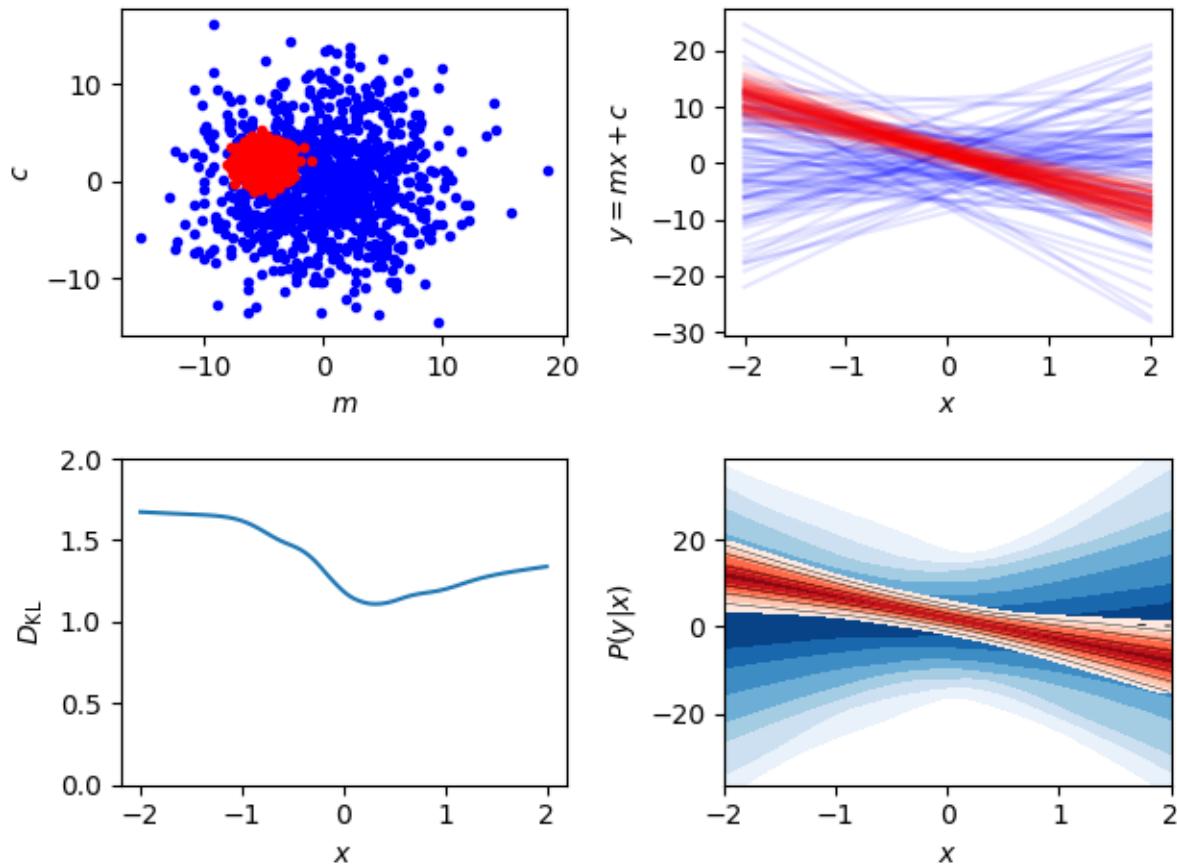
# Predictive posterior plot
# -----
ax_fgivenx = axes[1, 1]
ax_fgivenx.set_ylabel(r'$P(y|x)$')
ax_fgivenx.set_xlabel(r'$x$')
cbar = plot_contours(f, x, prior_samples, ax_fgivenx,
                      colors=plt.cm.Blues_r, lines=False,
                      cache=prior_cache)
cbar = plot_contours(f, x, samples, ax_fgivenx, cache=cache)

# DKL plot
# -----
ax_dkl = axes[1, 0]
ax_dkl.set_ylabel(r'$D_{\text{KL}}(\mathcal{P}(y|x) \parallel \mathcal{P}_{\text{true}}(y|x))$')
ax_dkl.set_xlabel(r'$x$')
ax_dkl.set_ylim(bottom=0, top=2.0)
plot_dkl(f, x, samples, prior_samples, ax_dkl,
          cache=cache, prior_cache=prior_cache)

ax_lines.get_shared_x_axes().join(ax_lines, ax_fgivenx, ax_dkl)

fig.tight_layout()
fig.savefig('plot.png')

```



## 10.6.2 Plot GetDist chains

```

import numpy
import matplotlib.pyplot as plt
from fgivenx import plot_contours, samples_from_getdist_chains

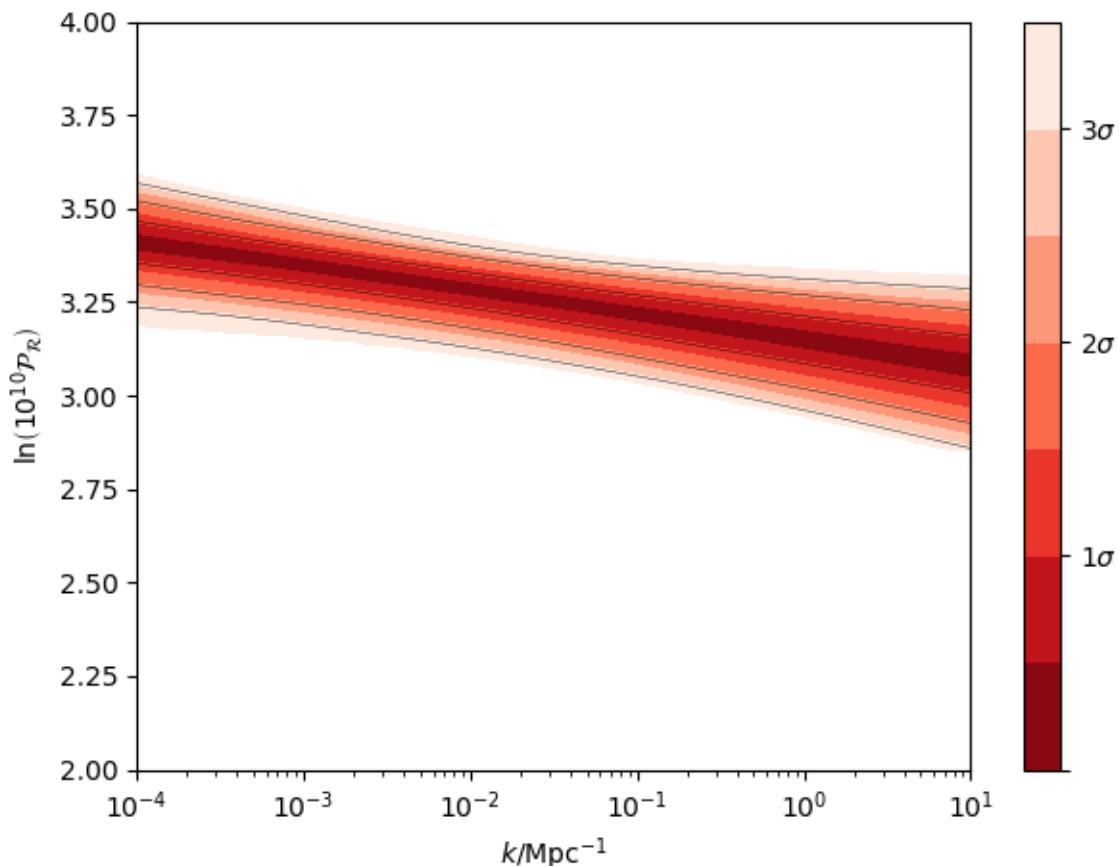
file_root = './plik_HM_TT_lowl/base_plikHM_TT_lowl'
samples, weights = samples_from_getdist_chains(['logA', 'ns'], file_root)

def PPS(k, theta):
    logA, ns = theta
    return logA + (ns - 1) * numpy.log(k)

k = numpy.logspace(-4, 1, 100)
cbar = plot_contours(PPS, k, samples, weights=weights)
cbar = plt.colorbar(cbar, ticks=[0, 1, 2, 3])
cbar.set_ticklabels(['', r'$1\sigma$', r'$2\sigma$', r'$3\sigma$'])

plt.xscale('log')
plt.ylim(2, 4)
plt.ylabel(r'$\ln\left(10^{10} \mathcal{P}_R\right)$')
plt.xlabel(r'$k / \rm Mpc^{-1}$')
plt.tight_layout()
plt.savefig('planck.png')

```



## 10.7 Contributing

Want to contribute to `fgivenx`? Awesome! There are many ways you can contribute via the [GitHub repository](<https://github.com/williamjameshandley/fgivenx>), see below.

### 10.7.1 Opening issues

Open an issue to report bugs or to propose new features.

### 10.7.2 Proposing pull requests

Pull requests are very welcome. Note that if you are going to propose drastic changes, be sure to open an issue for discussion first, to make sure that your PR will be accepted before you spend effort coding it.

## 10.8 Changelog

**v2.2.0** Paper accepted

**v2.1.17** 100% coverage

- v2.1.16** Tests fixes
- v2.1.15** Additional plot tests
- v2.1.13** Further bug fix in test suite for image comparison
- v2.1.12** Bug fix in test suite for image comparison
- v2.1.11** Documentation upgrades
- v2.1.10** Added changelog

---

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